

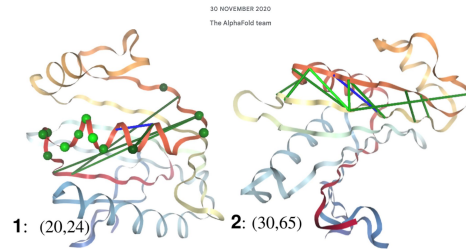
Generative Foundation Models for Sciences

Tung Nguyen, CS261 Winter 2024

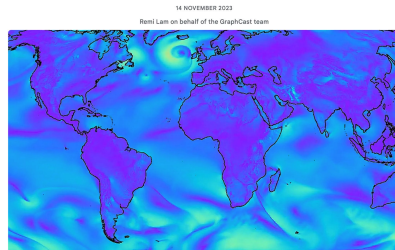


Science Advances by AI

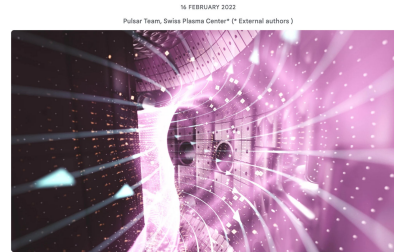
AlphaFold: a solution to a 50-year-old grand challenge in biology



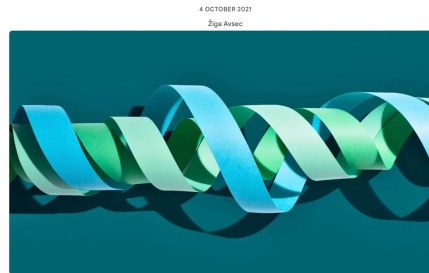
GraphCast: AI model for faster and more accurate global weather forecasting



Accelerating fusion science through learned plasma control



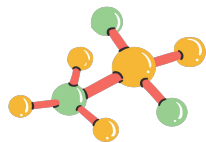
Predicting gene expression with AI



AI has the capability to discover and simulate complex patterns!

General Problem

Learn a surrogate model f_θ to approximate $y = f(x)$



Chemical molecules

|

$f(x)$

Reactivity, Stability

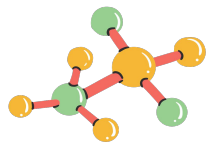
|

x

Formula, structure

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x

Formula, structure



Robotics

|

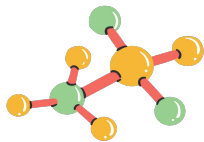
Speed, Energy

|

limbs, mass

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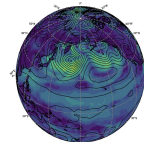
Robotics

|

Speed, Energy

|

limbs, mass



Climate Science

|

Future weather

|

Current weather

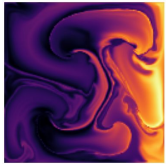
Surrogate Modeling Use Cases

Prediction

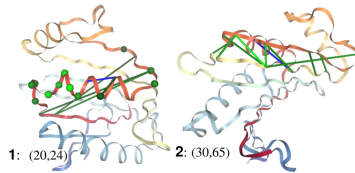
How to use $f_\theta(x)$ to **forecast/simulate** $f(x)$?



Weather forecasting



PDE
modeling

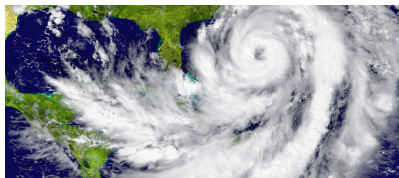


Protein structure
prediction

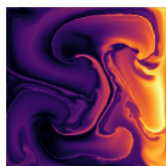
Surrogate Modeling Use Cases

Prediction

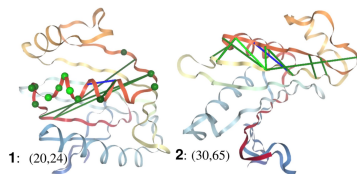
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Weather forecasting



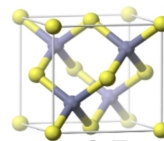
PDE modeling



Protein structure prediction

Black-box Optimization

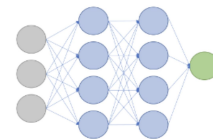
How to use $f_{\theta}(x)$ to **optimize** $f(x)$?



Material design



Molecular optimization

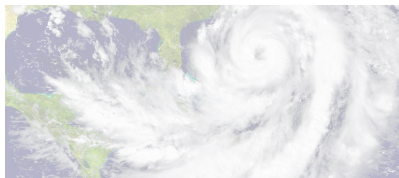


Hyperparameter optimization

Today's Talk

Prediction

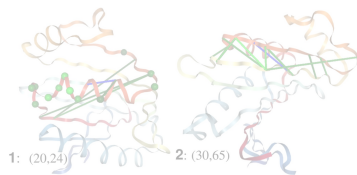
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Weather forecasting



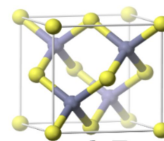
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Black-box Optimization

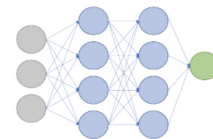
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Material design



Molecular optimization

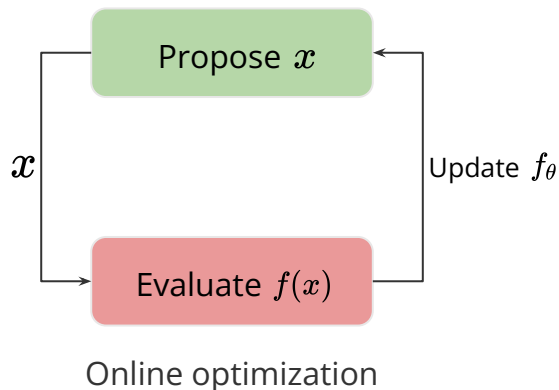


Hyperparameter optimization

Black-box Optimization

- General Problem: **Optimize** a function **without** its functional form or **gradient** information

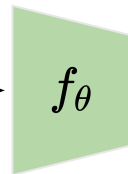
$$x^* = \operatorname{argmax} f(x)$$



Logged data
 $\{(x_i, y_i)\}_{i=1}^N$



Train



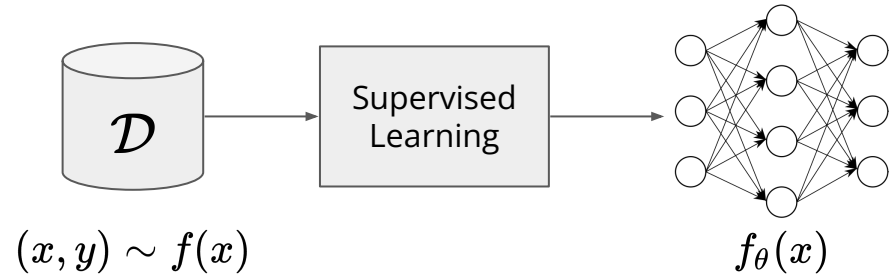
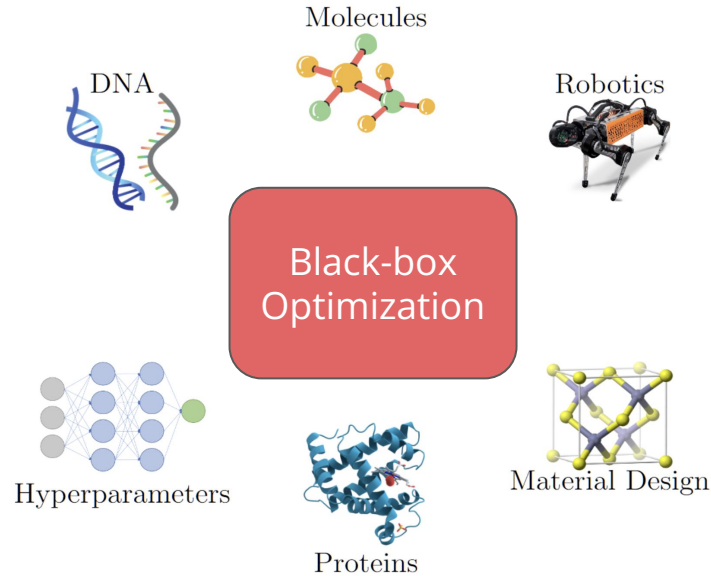
Optimize

x^*

Offline optimization

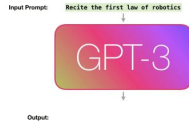
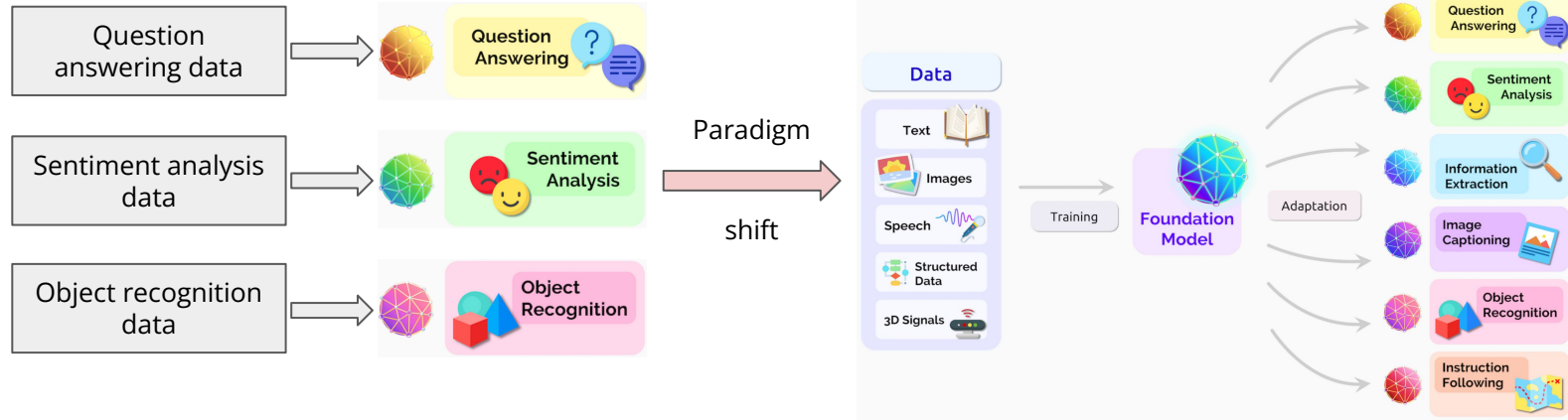
Limited labeled data but plenty unlabeled data!

Task-specific Surrogate Models



- ☐ Overfitting
- ☐ Train one network for each task
- ☐ Do not make use of unlabeled data

Foundation Models



language

[Vaswani et al., 2017;
Radford et al., 2019;
Brown et al., 2020;
inter alia]

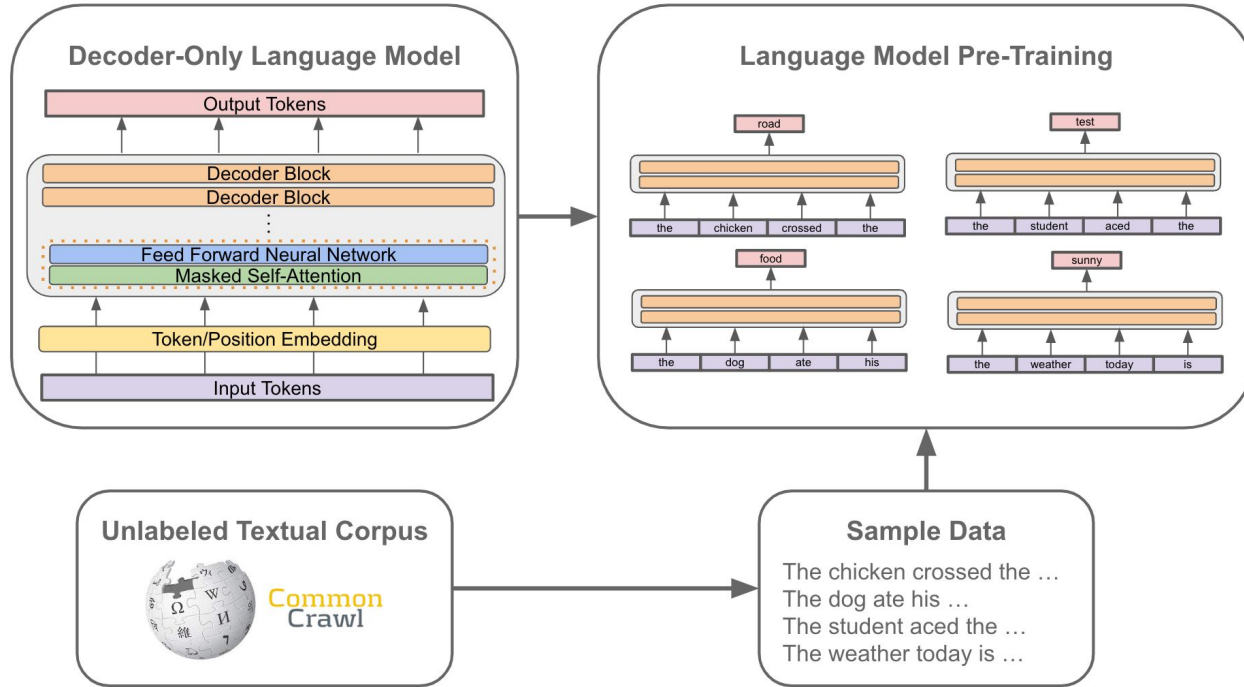


vision

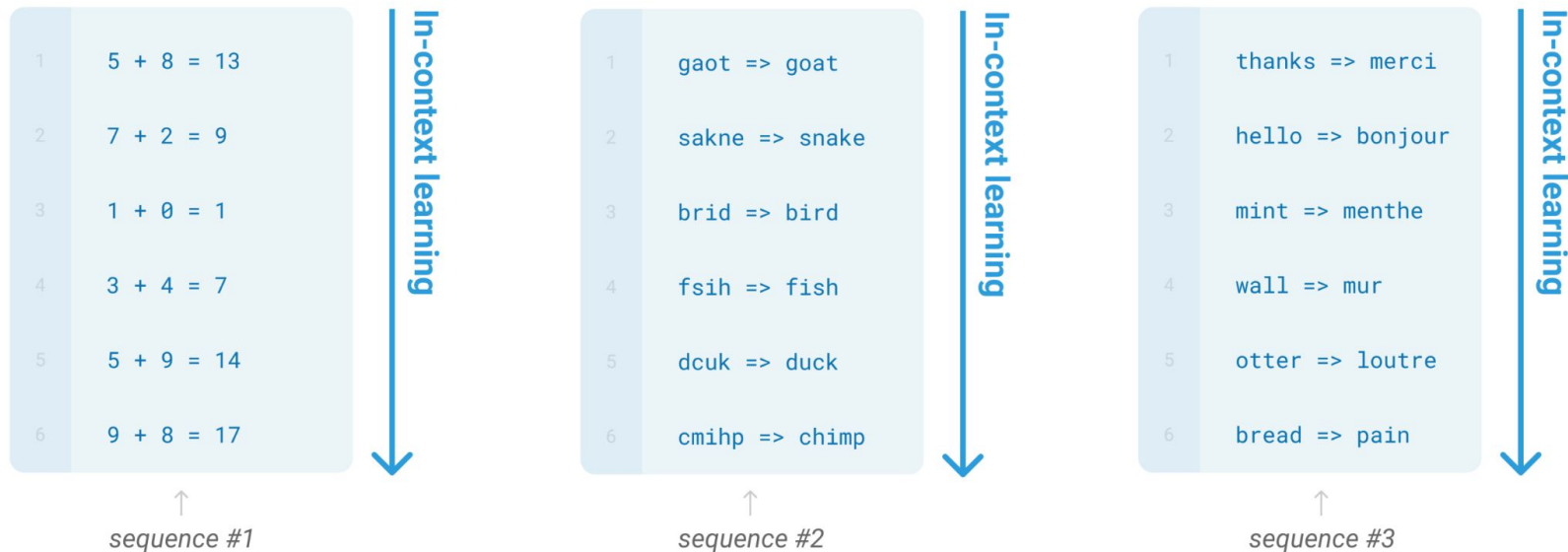
[Radford et al., 2019;
Ramesh et al., 2021;
Rombach et al., 2021;
inter alia]

- ❑ Unsupervised pretraining
- ❑ Efficiently generalize to unseen tasks

GPT-3 Pretraining

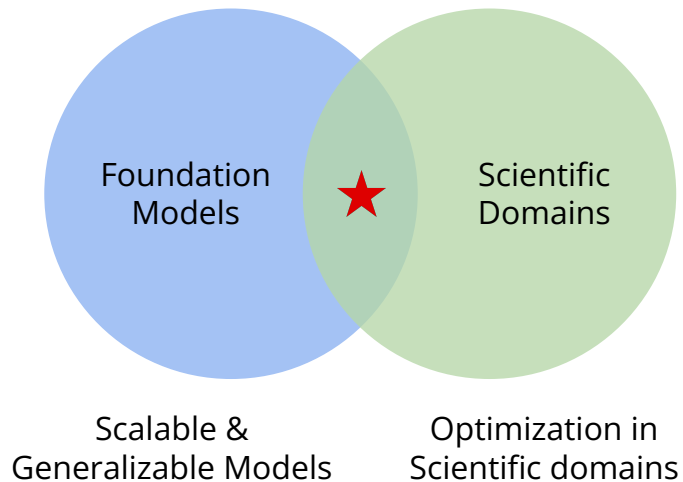


GPT-3 In-context Learning



Emergent in-context learning!

Today's Talk



★ Today's talk

Foundation Models for Sciences

Today's Talk

❏ **Part 1:** Learning to Learn In-context

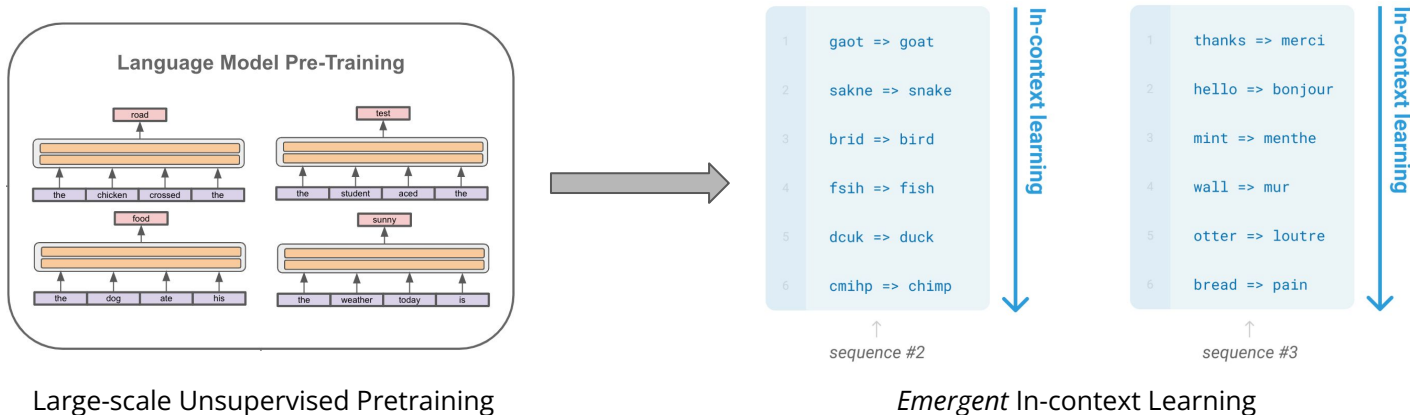
*How to train a model that **generalizes** to **unseen functions** via **in-context conditioning**?*

❏ **Part 2:** Cross-domain In-context Learning

How to leverage a pretrained LLM for in-context learning in an unseen domain?

Today's Talk

- ❑ **Question:** How to train a model to **generalize** to unseen **functions/tasks**?
- ❑ In-context learning is an *emergent capability* of GPT-3 at a certain scale



Can we *explicitly* train a model to generalize to unseen functions?

Generalizing over Functions

- ❑ **Question:** How to train a model to **generalize** to unseen **functions/tasks**?

Data Points Generalization

- ❑ Learning over data points drawn from the same function

$$\mathbb{E}_{x \sim p_{\text{train}}(x), y=f(x)} [\log p(y \mid x)]$$

- ❑ The model generalizes to unseen data points

$$x \sim p_{\text{test}}(x), y = f(x)$$

Generalizing over Functions

- ❑ **Question:** How to train a model to **generalize** to unseen **functions/tasks**?

Data Points Generalization

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- ❑ The model generalizes to unseen data points

$$x \sim p_{\text{test}}(x), y = f(x)$$

Functional Generalization

- ❑ Learning over functions, given finite context of labeled points

$$\mathbb{E}_{f \sim \mathcal{F}_{\text{train}}, (x,y), C \sim f} [\log p(y \mid x, C)]$$

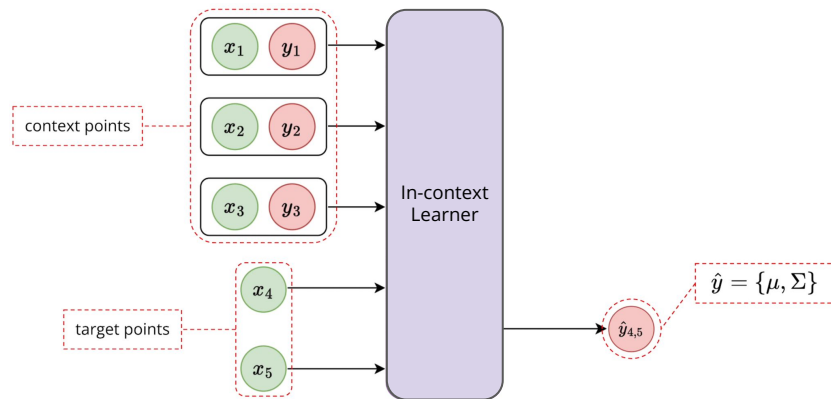
- ❑ The model generalizes to unseen functions given the context

$$f \sim \mathcal{F}_{\text{test}}, (x, y), C \sim f$$

Learning to learn in-context

Learning to Learn In-context

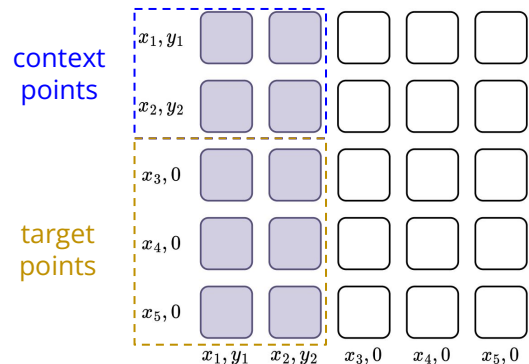
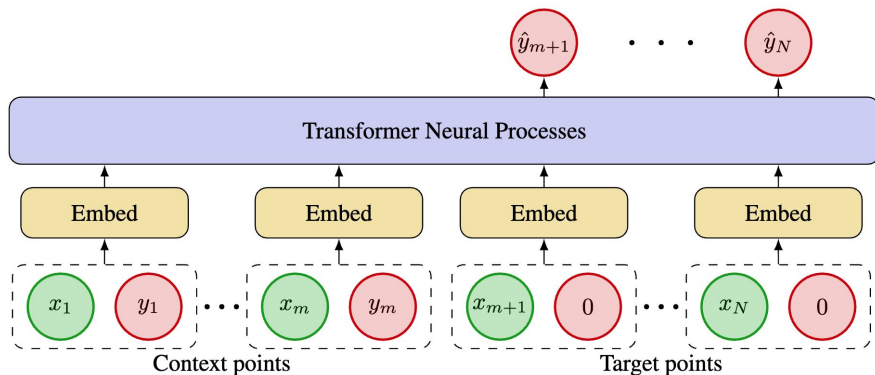
- ❑ Sample $f \sim \mathcal{F}_{\text{train}}$ and $x_{1:N}, y_{1:N} \sim f$
- ❑ Observe context points $\{x_i, y_i\}_{i=1}^m$ and make predictions for a set of target points $\{x_j\}_{j=m+1}^N$.



$$\mathcal{L}(\theta) = \mathbb{E}_{f \sim \mathcal{F}_{\text{train}}, x_{1:N}, y_{1:N} \sim f, m} [\log p_{\theta} (\underbrace{y_{m+1:N}}_{\text{target outputs}} \mid \underbrace{x_{m+1:N}}_{\text{target inputs}}, \underbrace{x_{1:m}, y_{1:m}}_{\text{context points}})]$$

Model Architecture

- We instantiate the framework with a **transformers** architecture called **TNP**



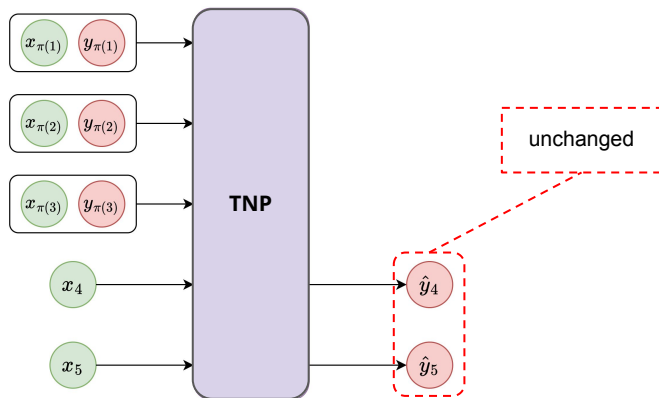
An example mask with $N=5$ and $m=2$

$$\begin{aligned} \mathcal{L}(\theta) &= \mathbb{E}_{f \sim \mathcal{F}_{\text{train}}, x_{1:N}, y_{1:N} \sim f, m} [\log p_{\theta}(y_{m+1:N} \mid x_{m+1:N}, x_{1:m}, y_{1:m})] \\ &= \mathbb{E}_{f \sim \mathcal{F}_{\text{train}}, x_{1:N}, y_{1:N} \sim f, m} \left[\sum_{i=m+1}^N \log p(y_i \mid x_i, x_{1:m}, y_{1:m}) \right] \end{aligned}$$

Properties of TNP

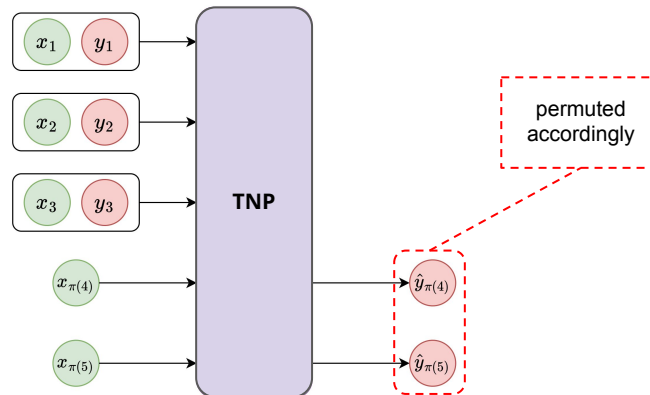
Property 1. Context invariance.

The model's predictions do not depend on the permutation of the context points.



Property 2. Target equivariance.

Whenever we permute the target inputs, the predictions are permuted accordingly.



Variants of TNPs

We introduce TNP-A and TNP-ND to improve expressivity

Autoregressive TNP (TNP-A)

Predict the target jointly with an autoregressive factorization:

$$\begin{aligned} p_{\theta}(y_{m+1:N} \mid x_{1:N}, y_{1:m}) \\ = \prod_{i=m+1}^N p_{\theta}(y_i \mid x_{1:i}, y_{1:i-1}) \end{aligned}$$

Non-Diagonal TNP (TNP-ND)

Predict the target jointly using a multivariate Gaussian distribution with a non-diagonal covariance matrix:

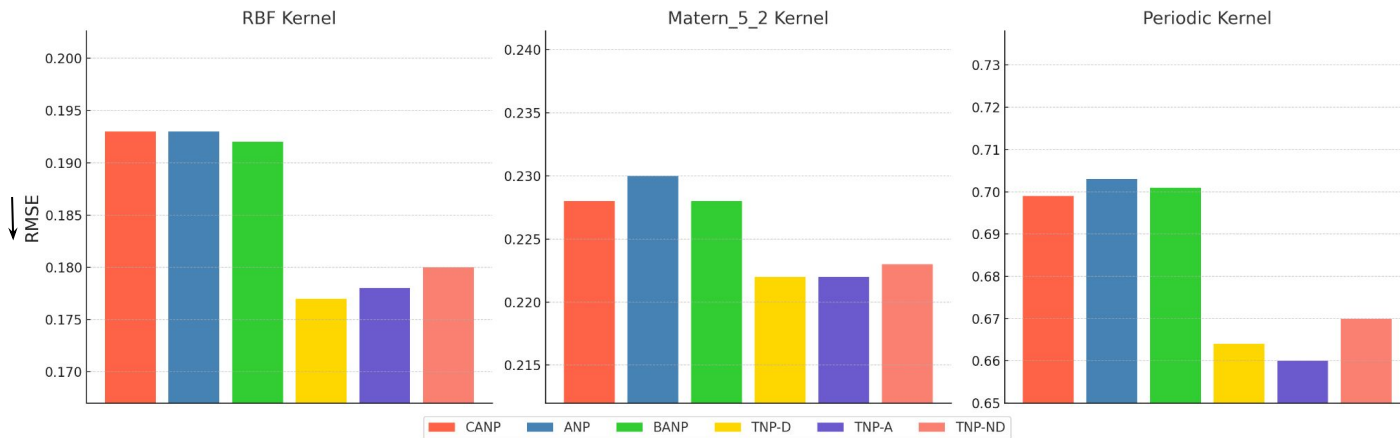
$$\begin{aligned} p_{\theta}(y_{m+1:N} \mid x_{1:N}, y_{1:m}) \\ = \mathcal{N}(y_{m+1:N} \mid \mu_{\theta}(x_{1:N}, y_{1:m}), \Sigma_{\theta}(x_{1:N}, y_{1:m})) \end{aligned}$$

TNPs for 1D Regression

- ❑ Train on functions generated from **GPs** with an **RBF kernel**

$$f \sim \mathcal{GP}(0, \mathcal{K}), \quad \mathcal{K}(x, x') = \sigma^2 \exp\left(-\frac{(x-x')^2}{2\ell^2}\right)$$

- ❑ Test on functions generated from **GPs** with **different kernels**

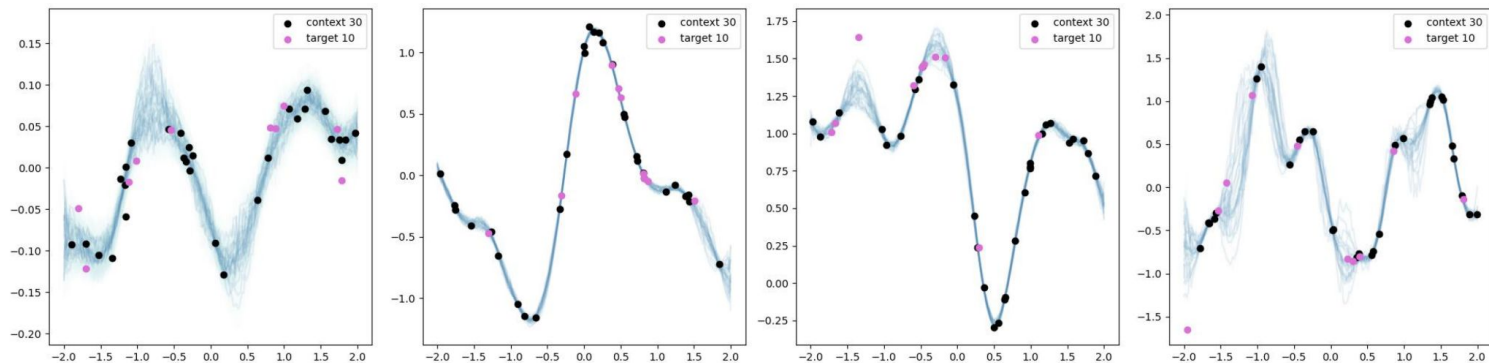


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- ❑ Test on functions generated from **GPs** with **different kernels**



TNP generalizes well to unseen functions!

TNPs for Image Completion

- ❑ Train to map from pixel coordinates $\rightarrow$ pixel values
- ❑ Each image is a 2-dimensional function

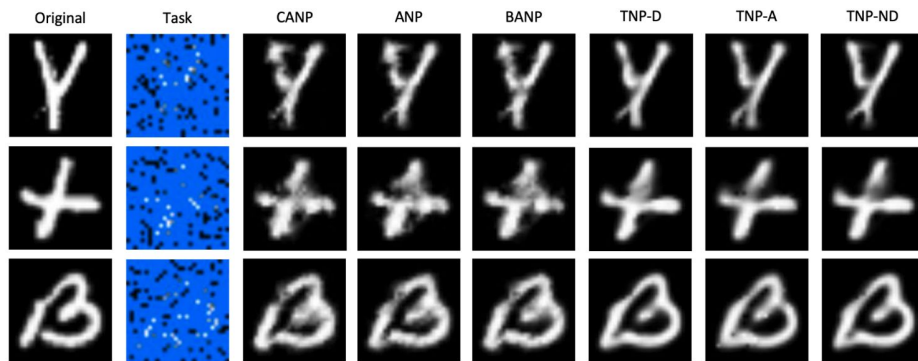
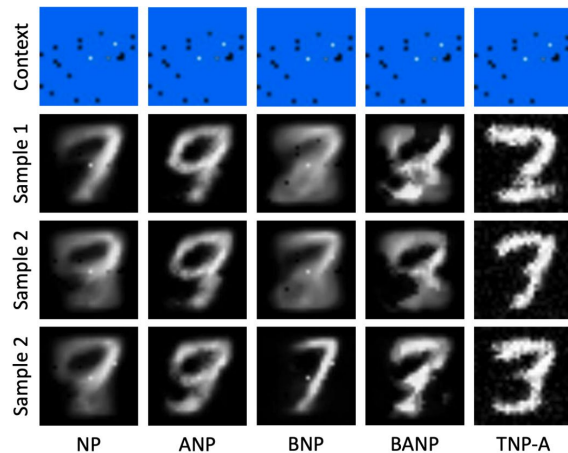


Image completion on unseen classes from 100 pixels



Samples from 20 context points.

Discussion

- ❑ TNP learns to learn in-context **from scratch**
 - ❑ It's often desired in deep learning to start from a pretrained model
- ❑ There exists powerful in-context models in other domains, e.g., large language models.

*Can we **transfer** in-context learning from **LLMs** to **new domains**?*

Today's Talk

❏ **Part 1:** Learning to Learn In-context ✓

*How to train a model that **generalizes** to **unseen functions** via **in-context conditioning**?*

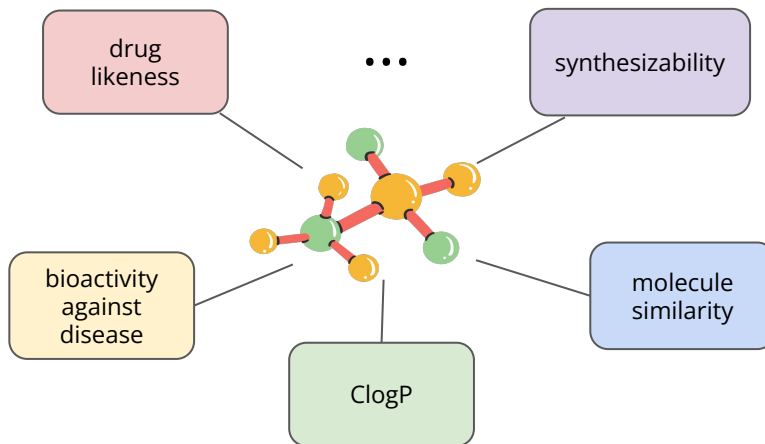
❏ **Part 2:** Cross-domain In-context Learning

How to leverage a pretrained LLM for in-context learning in an unseen domain?

Molecular Optimization

- ❑ Problem: find the molecule that optimizes a certain property.

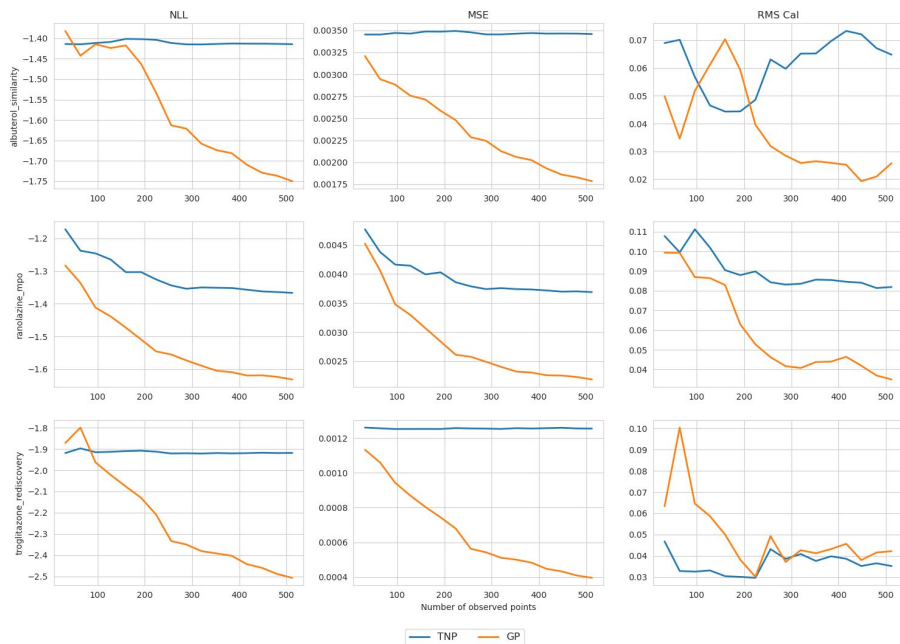
$$x^* = \arg \min_{x \in \mathcal{X}} f(x)$$



- ❑ Important domain and distinguished from language.

TNPs for Molecular Optimization

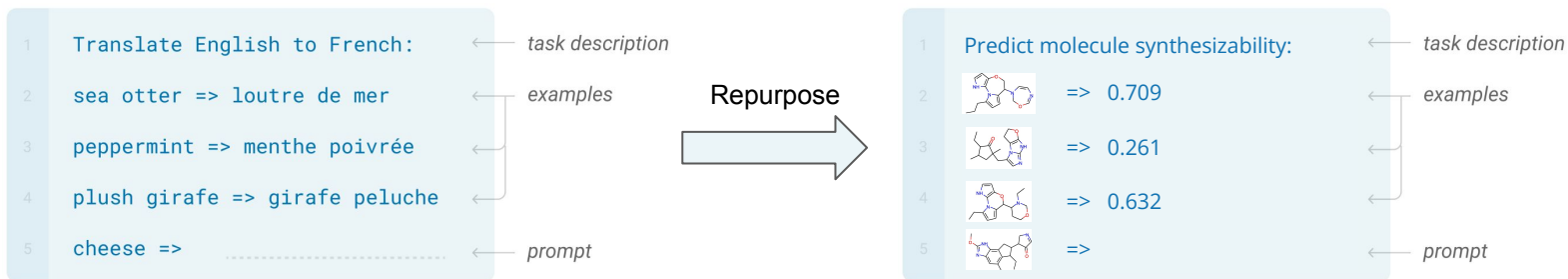
- ❑ First attempt: TNPs for in-context molecular property prediction



Solution: Use a more capable model,
i.e., a pretrained LLM

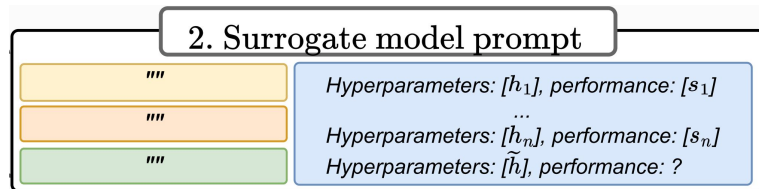
LLMs for Molecular Optimization

- ❑ Motivation: Repurpose a pretrained LLM for in-context learning in a new domain.



LLMs for Optimization

- ❑ Existing works directly prompt a pretrained LLM in the text space.
 - ❑ Not applicable to non-textual domains ✖
 - ❑ Do not generalize to underrepresented domains ✖



Liu, Tennison, et al. "Large Language Models to Enhance Bayesian Optimization." *arXiv preprint arXiv:2402.03921* (2024).

Your task is to generate the instruction <INS>. Below are some previous instructions with their scores. The score ranges from 0 to 100.

text:

Let's figure it out!

score:

61

text:

Let's solve the problem.

score:

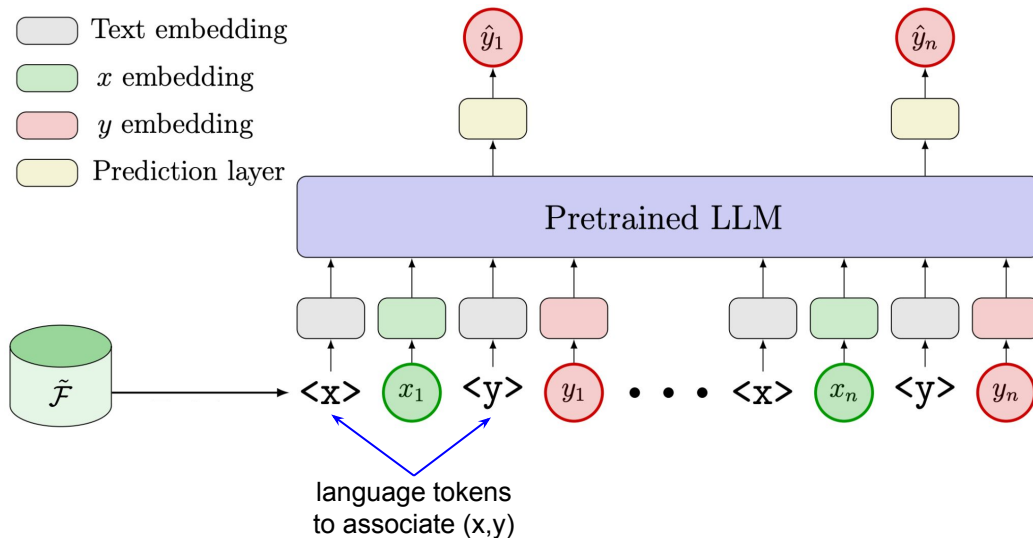
63

Generate an instruction that is different from all the instructions <INS> above, and has a higher score than all the instructions <INS> above. The instruction should begin with <INS> and end with </INS>. The instruction should be concise, effective, and generally applicable to all problems above.

Yang, Chengrun, et al. "Large language models as optimizers." *arXiv preprint arXiv:2309.03409* (2023).

BOLM Architecture

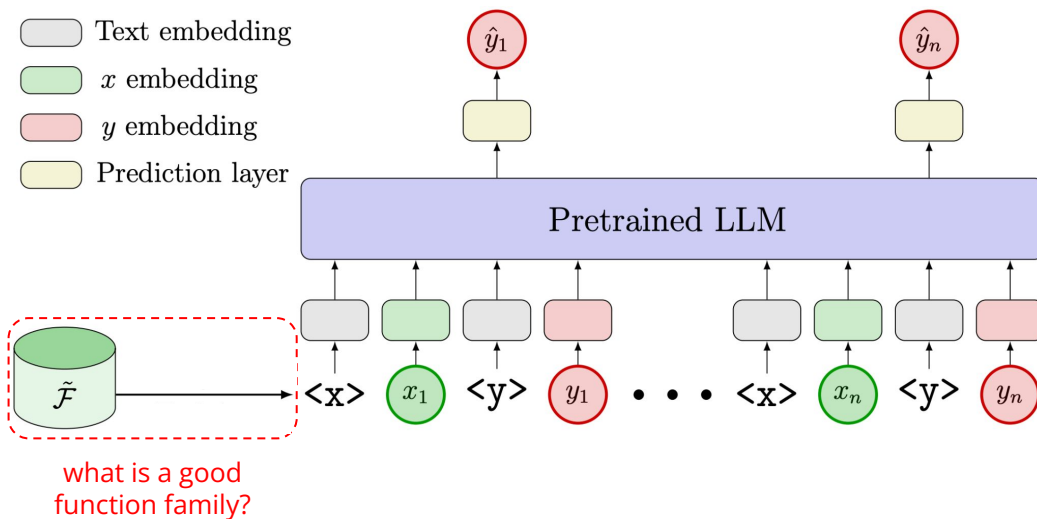
- ❑ Learn separate embedding and prediction layers for the new domain
 - ❑ Domain-agnostic ✓
 - ❑ Computationally efficient ✓



BOLM Training

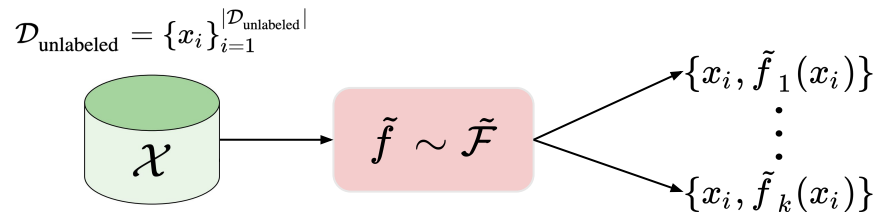
- ❑ Train BOLM to perform in-context learning prediction

$$\mathcal{L}(\theta) = \mathbb{E}_{\tilde{f} \sim \tilde{F}, x_{1:N}, y_{1:N}} \left[\sum_{i=1}^N \log p_{\theta}(y_i \mid x_i, x_{<i}, y_{<i}) \right]$$



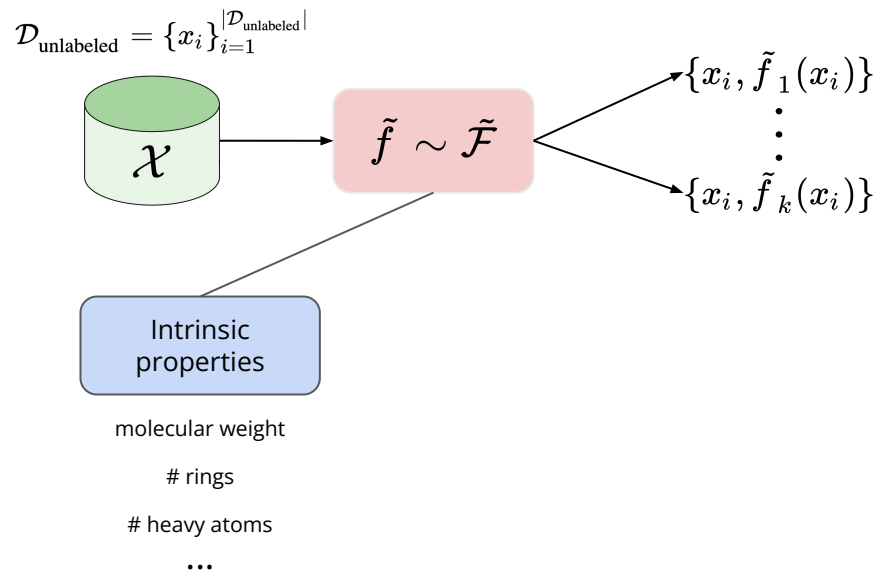
Training Data Generation

- ❑ Ideal family of functions $\tilde{\mathcal{F}}$
 - ❑ Close to downstream functions
 - ❑ Diverse



Training Data Generation

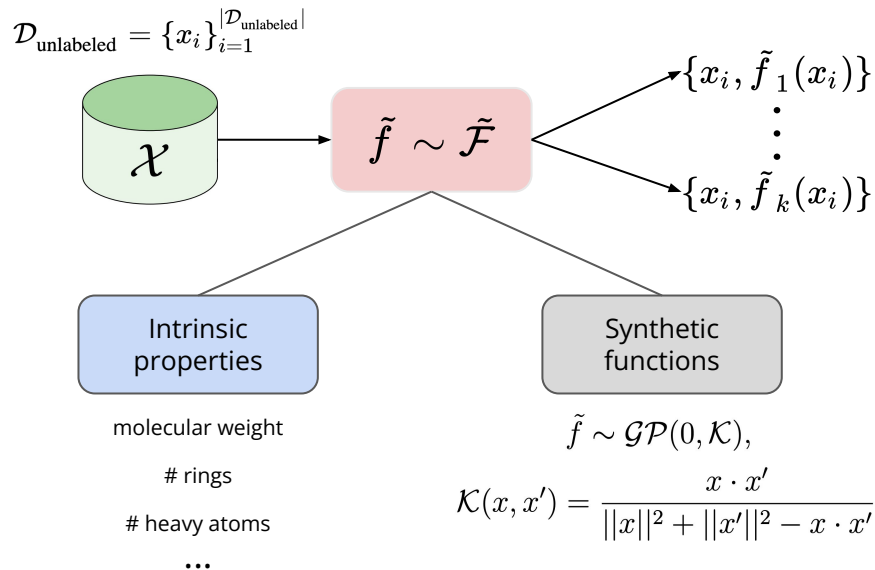
- ❑ Ideal family of functions $\tilde{\mathcal{F}}$
 - ❑ Close to downstream functions ✓
 - ❑ Diverse



Training Data Generation

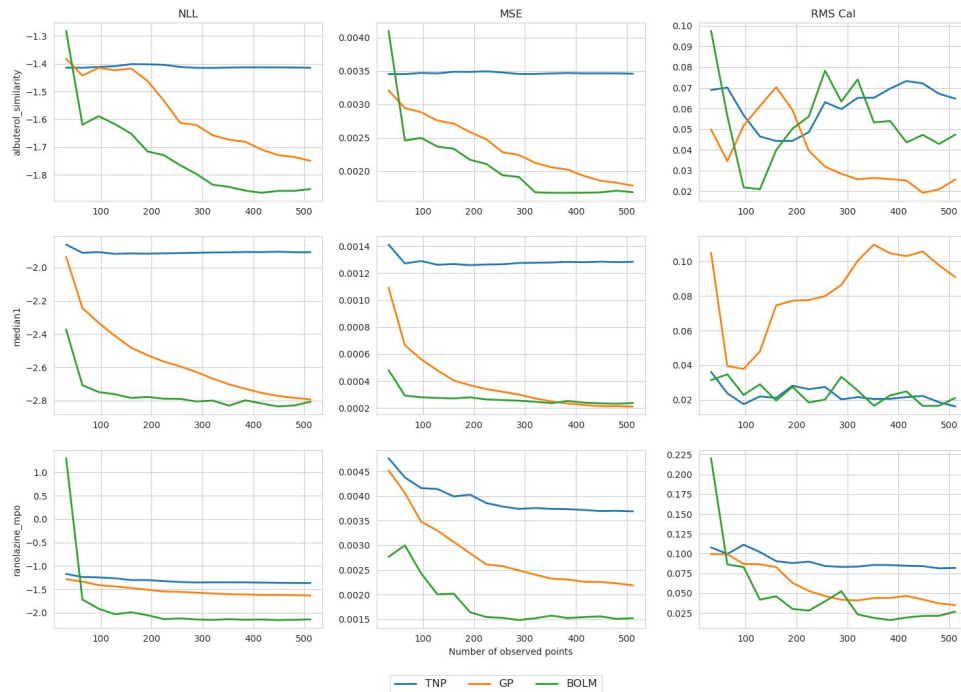
- ❑ Ideal family of functions $\tilde{\mathcal{F}}$
 - ❑ Close to downstream functions ✓
 - ❑ Diverse ✓

Semi-synthetic training!



Prediction Results

❑ Test BOLM on in-context molecular property prediction



BOLM for Black-box Optimization

- ❑ We ultimately care about optimization
- ❑ We consider the online setting

Algorithm 1 Black-box optimization with BOLM

Require: objective f , fine-tuned LLM surrogate f_θ , budget B , candidate pool size C , acquisition function α , batch size k

Initialize $\mathcal{D}_{\text{obs}} = \{\}$

while $|\mathcal{D}_{\text{obs}}| < B$ **do**

Generate a set of candidates $\{x_i\}_{i=1}^C$

Evolutionary

for each candidate x_i **do**

Predict $\mu_i, \sigma_i = f_\theta(x_i, \mathcal{D}_{\text{obs}})$

BOLM

Compute utility score $u_i = \alpha(\mu_i, \sigma_i)$

UCB

end for

Select k candidates with the highest utility scores

for each selected candidate x_j **do**

Evaluate x_j using the actual objective $y_j = f(x_j)$

Add (x_j, y_j) to the observation dataset $\mathcal{D}_{\text{obs}}$

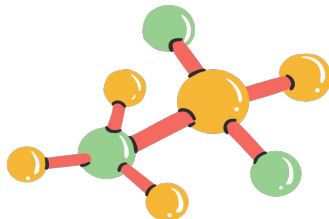
end for

end while

PMO Benchmark

- ❑ We test (a single) BOLM on 21 benchmark optimization tasks from PMO

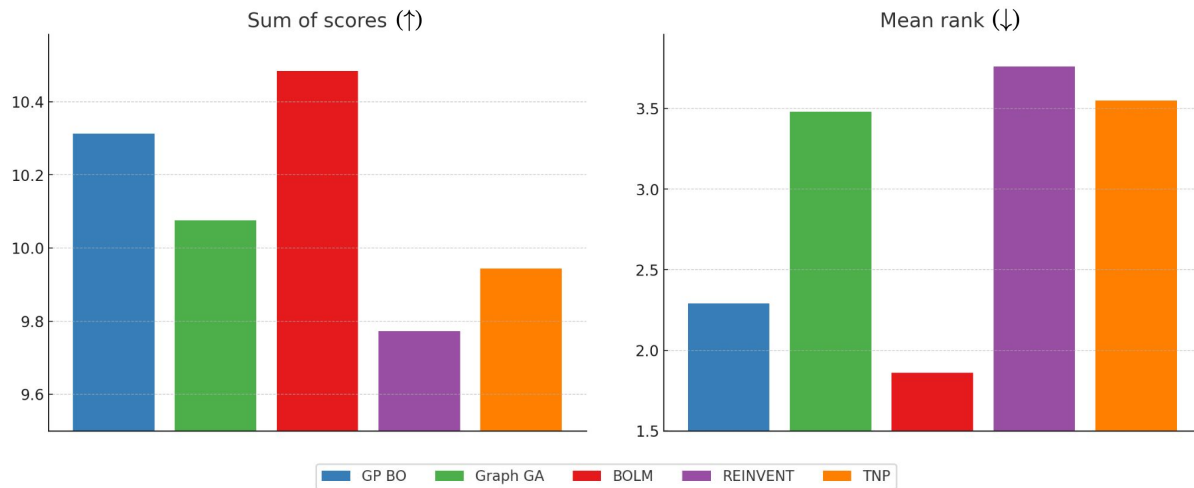
Task
albuterol_similarity
amlodipine_mpo
celecoxib_rediscovery
deco_hop
drd2
fexofenadine_mpo
isomers_c7h8n2o2
isomers_c9h10n2o2pf2cl
median1
median2



Task
mestranol_similarity
osimertinib_mpo
perindopril_mpo
qed
ranolazine_mpo
scaffold_hop
sitagliptin_mpo
thiothixene_rediscovery
trogliatazone_rediscovery
valsartan_smarts
zaleplon_mpo

Experiments

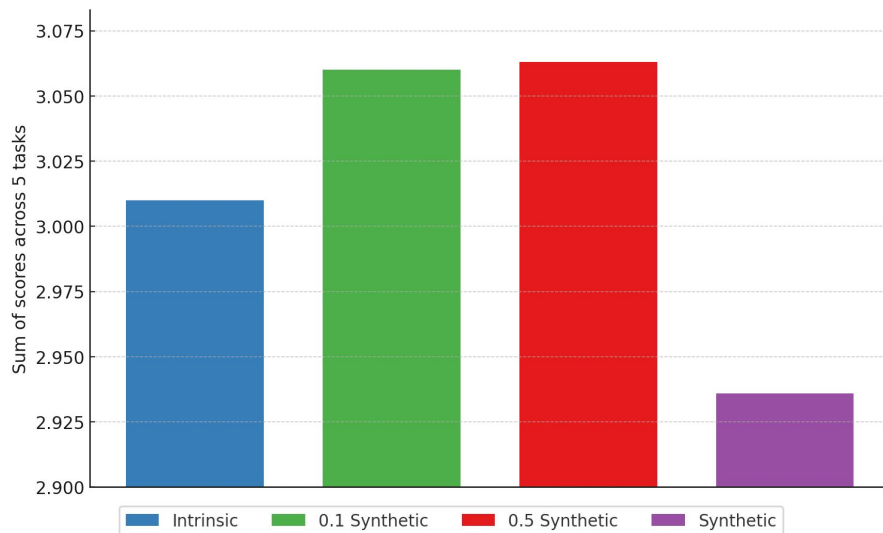
- ❑ We test (a single) BOLM on 21 benchmark optimization tasks



BOLM achieves the best overall scores and ranking!

Ablation Studies

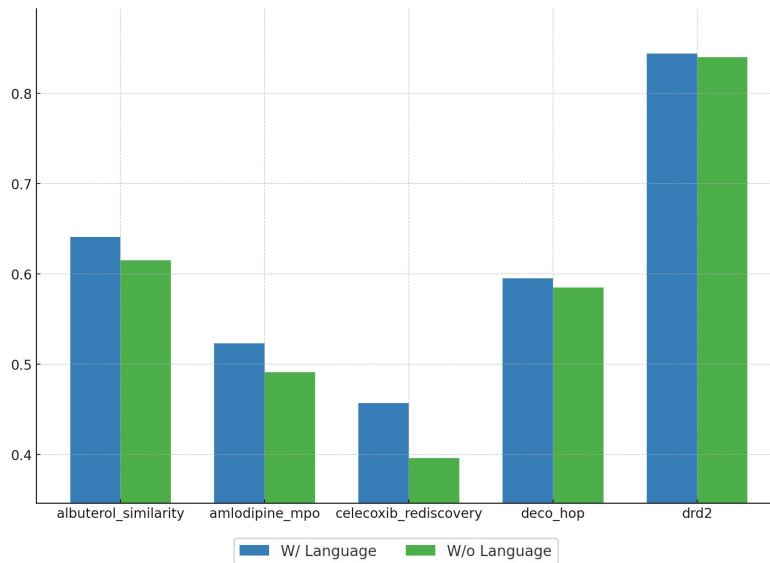
❑ Importance of semi-synthetic training



Semi-synthetic is better than intrinsic or synthetic alone

Ablation Studies

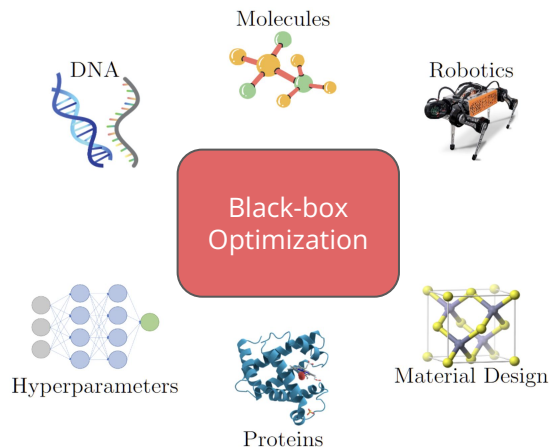
❑ Importance of language instruction



Language instruction is crucial to BOLM

Summary

- ❑ We can train a model to learn in-context
 - ❑ In-context learning can **generalize** from **synthetic to real** functions
 - ❑ In-context learning can be **transferred across domains**
- ❑ End goal: have a GPT-like model that scientists can use to optimize **arbitrary objectives**



Future Work

- ❑ Improve generality
 - ❑ Foundation models that can perform cross-domain optimization
- ❑ Improve performance
 - ❑ Scale up data and model size
 - ❑ Parameter-efficient finetuning
- ❑ Foundation models for end-to-end optimization
 - ❑ Candidate generation, exploration, surrogate modeling, etc.

Thank You!
Q&A