

# Lecture 2: Functions

CS 61A - Summer 2024

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$$20 + 24$$

$$2^{100}$$

$$\sin \pi$$

$$\lim_{x \rightarrow \infty} \frac{1}{x}$$

$$f(x)$$

$$\log x$$

$$\frac{20}{24}$$

$$\sum_{i=1}^n i$$

$$\sqrt{2024}$$

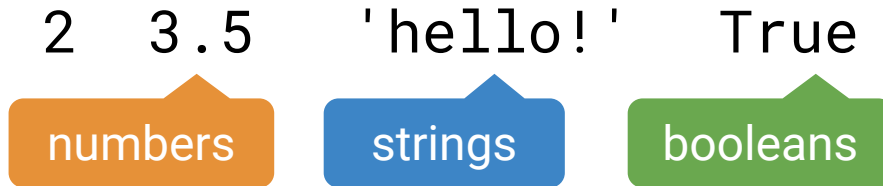
$$\binom{n}{x}$$

$$-2024$$

An **expression** describes a computation and evaluates to a value.

# Types of Expressions

**Primitive Expressions:**



**Call Expressions:**



# Call Expressions

Evaluation procedure for **call expressions**

1. Evaluate the **operator**
2. Evaluate the **operands** from left to right
3. **Apply** the operator (a **function**) to the evaluated operands (**arguments**)



Operators and operands are also expressions

So they also *evaluate to values*

add(add(6, mul(4, 6)), mul(3, 5))

Operator

Operand

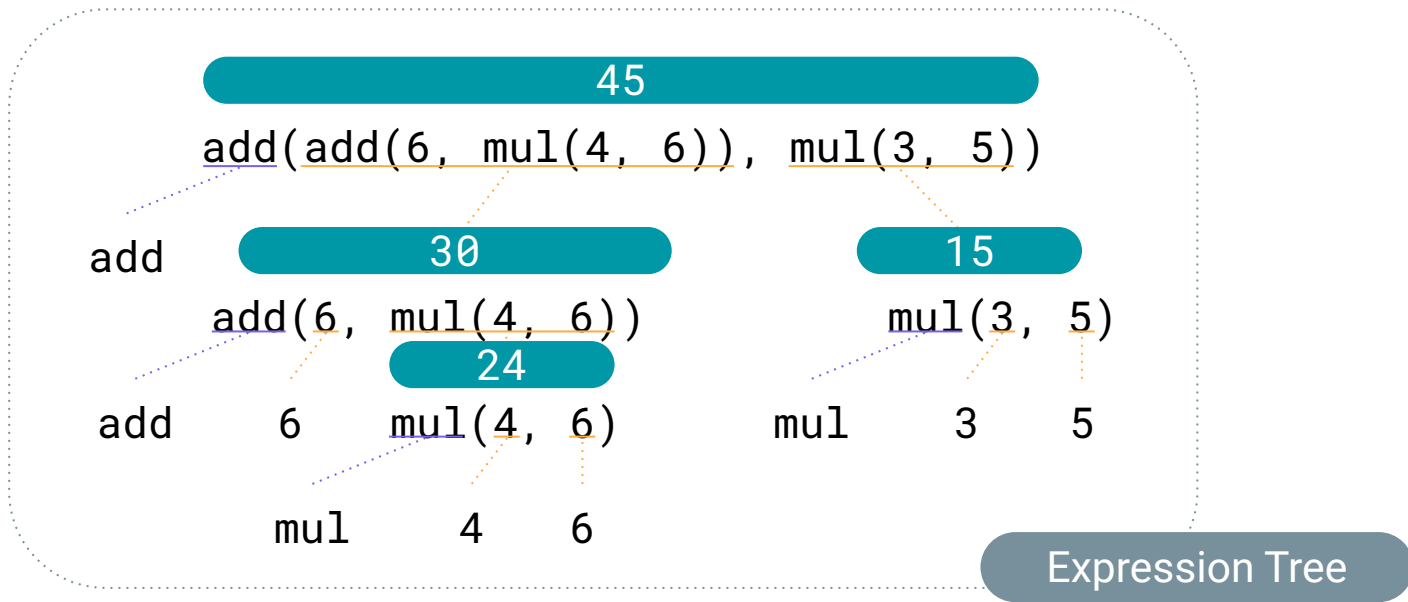
Operand

# Nested Call Expressions

1 Evaluate operator

## 2 Evaluate operands

### 3 Apply!



# Assignment Statements

In Python, we can bind expressions to variables.

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Assignment Statement



```
x = 1 + 2
```



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Assignment Statement



The diagram shows the assignment statement `x = 1 + 2` enclosed in a dotted rectangular box. A curved line connects the text 'Assignment Statement' to the left side of the box. Two straight lines point from the bottom of the box to the text 'Bound to the variable on the left' and 'Expression on the right'.

```
x = 1 + 2
```

Bound to  
the variable  
on the left

Expression on the  
right

# Assignment Statements

In Python, we can bind expressions to variables.

Assignment Statement

$x = 1 + 2$

Bound to  
the variable  
on the left

Expression on the  
right

Incorrect!

$1 + 2 = x$

# Assignment Statements – Example

```
>>> x = 2
>>> y = x + 1
>>> y
3
>>> x = 5
>>> y
3
```

# Assignment Statements – Example

```
>>> x = 2
>>> y = x + 1
>>> y
3
>>> x = 5
>>> y
3
```

y still retains its  
original value  
after x has been  
reassigned!

# Demo: Assignment of Python builtin functions

# User Defined Functions

We can define our own functions using `def` statements!

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```
def square(x):  
    """  
    Takes an input x and squares it.  
    >>> square(3)  
    9  
    """  
    return pow(x, 2)
```

# User Defined Functions

We can define our own functions using def statements!

def tells Python  
we're defining a  
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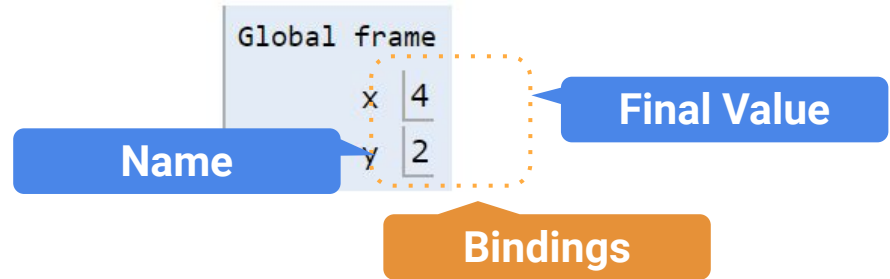
A function's **signature** is denoted as the name of the function and the arguments it takes in.

# Environment Diagrams

# Visualizing Assignment

Names are bound to **values** in an **environment**

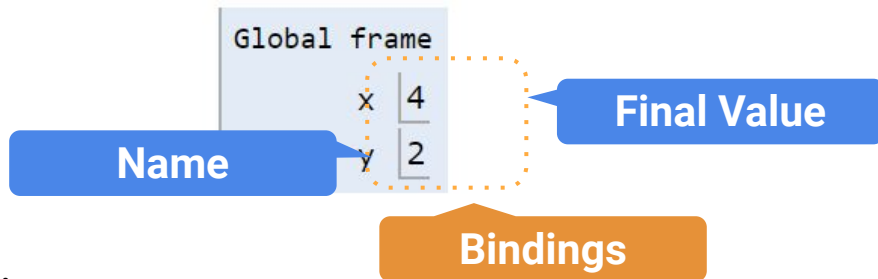
```
1 x = 1
2 y = 2
3 x = y * 2
```



# Visualizing Assignment

Names are bound to **values** in an **environment**

```
1  x = 1
2  y = 2
3  x = y * 2
```



To execute an assignment statement:

1. **Evaluate** the expression to the right of **=**.
2. **Bind** the value of the expression to the name to the left of **=** in the current environment.

# Calling User Defined Functions

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Write code in  and

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3     Takes an input x and squares it.
4     >>> square(3)
5     9
6     """
7     return pow(x, 2)
8
9 square(2)
```

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# Calling User Defined Functions

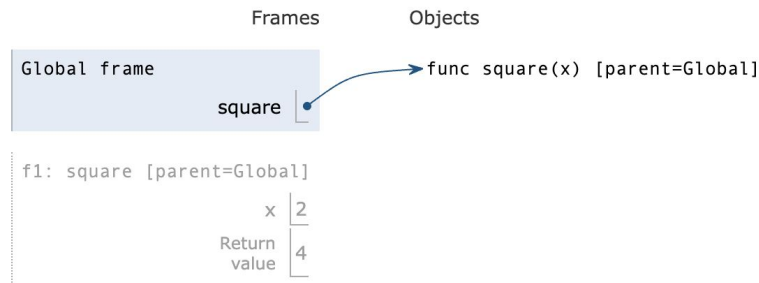
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Write code in Python 3.6 ▾ and display frames of exited functions. ▾

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# Calling User Defined Functions

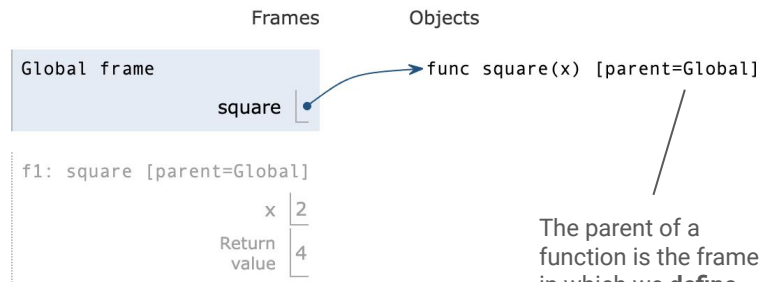
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The parent of a function is the frame in which we **define** the function

# Calling User Defined Functions

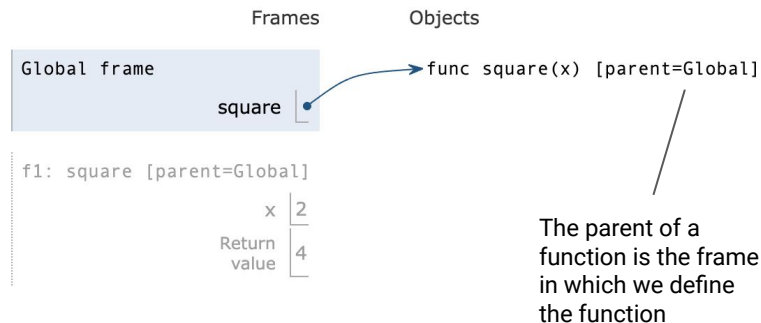
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```

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\*A function's signature has all the information needed to create a local frame

\*Except argument values

Break time!

What if we have variables with the same name in different parts of our program?

```
x = 1
def my_func():
    x = 100
    print(x)
```

```
my_func() # What value gets displayed here?
```



What if we have variables with the same name in different parts of our program?

```
x = 1
def my_func():
    x = 100
    print(x)

my_func() # What value gets displayed here?
```

Answer: 100

# Looking Up Names in Environments

**Every expression is evaluated in the context of an environment.**

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1. ***An environment is a sequence of frames.***

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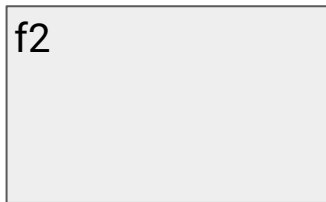
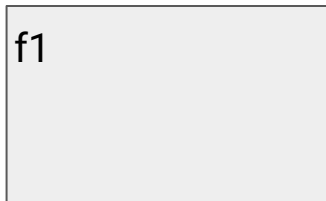
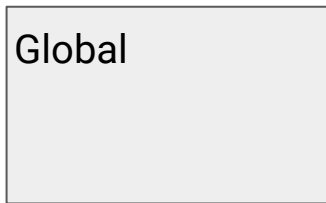
Our programs always begin with a *global* frame, and then new *local* frames are created when we make a function call.

Most important rules for environment diagrams:

1. ***An environment is a sequence of frames.***
2. ***A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found***

# A sequence of frames

Latest



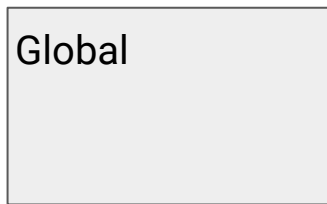
Earliest

•

•

# A sequence of frames

Latest



Earliest

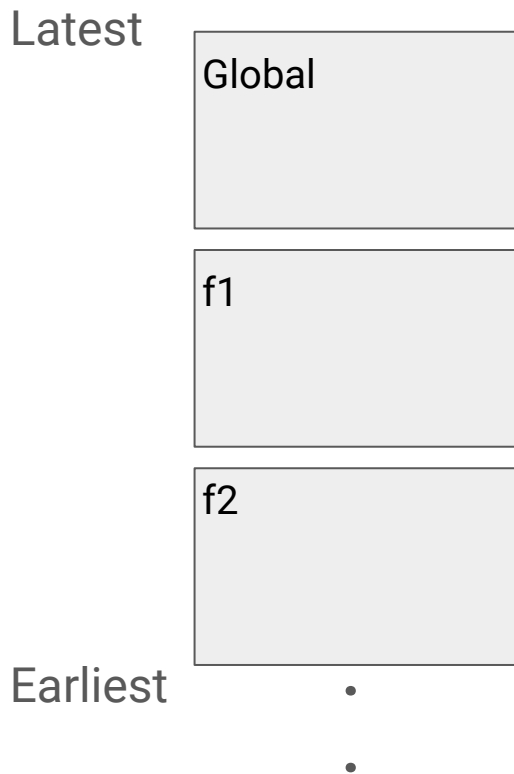
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A sequence is a first frame, and then the rest of the sequence



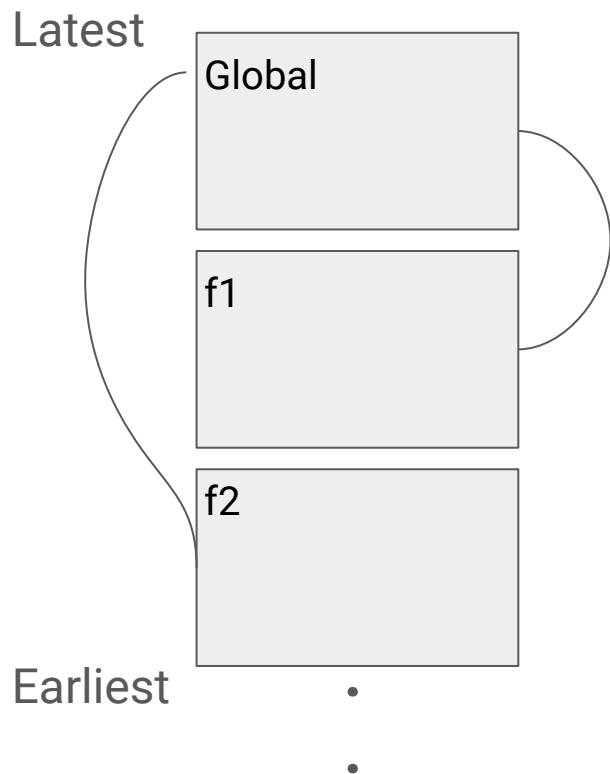
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Not every frame is part of the same environment, though each frame on the left is part of the **environment diagram**

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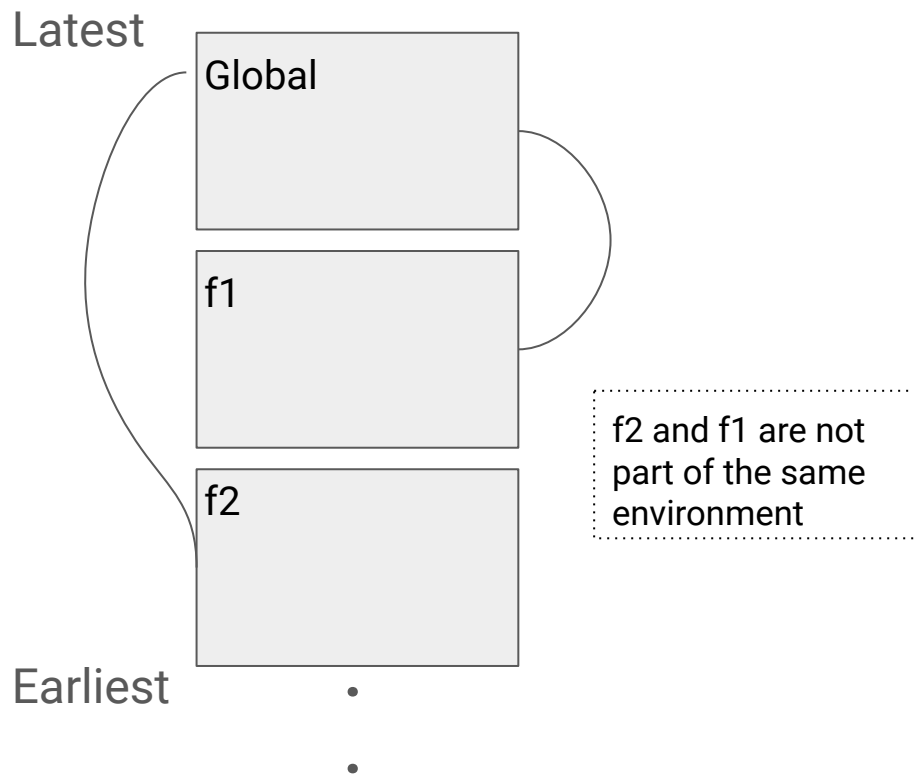


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f2 has a parent frame of Global, and f1 has a parent frame of Global

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A sequence is a first frame, and then the rest of the sequence

Not every frame is part of the same environment, though each frame on the left is part of the **environment diagram**

f2 has a parent frame of Global, and f1 has a parent frame of Global

## Example #1

```
x = 4
def f():
    x = 2
    return x + 1

def g():
    y = 2
    return x + y

f()
print(g()) # What value gets displayed here?
```

## Example #1

```
x = 4
def f():
    x = 2
    return x + 1

def g():
    y = 2
    return x + y

f()
print(g()) # What value gets displayed here?
```

**Answer: 6**

## Example #2

```
from operator import mul

def square(square):
    return mul(square, square)

print(square(3))
```

# Reminder: Rules for evaluating call expressions

Evaluation procedure for **call expressions**

1. Evaluate the **operator**
2. Evaluate the **operands** from left to right
3. **Apply** the operator (a **function**) to the evaluated operands (**arguments**)

***It is not until we finish the first two steps and get to the third step that a new frame is opened, and operand values are bound to the argument names!***

## Example #2

```
from operator import mul

def square(square):
    return mul(square, square)

print(square(3))
```

Answer: 9



# Summary

- An **expression** is anything that evaluates to a value in Python
  - Primitive and call expressions
- **Assignment statements** bind names to values
- Call expression evaluation follows a distinct set of rules
  - Evaluate the operator, evaluate the operand, and apply the operator onto the operands
- **Environment diagrams** allow us to visualize assignment
  - Use [tutor.cs61a.org](http://tutor.cs61a.org) to try this out on your own programs!
- Each environment is a sequence of frames, and all frames in a program make up an environment diagram